

# Use of Three-Cornered Hat Error Estimates in MERRA-2 to Guide an Improved Reanalysis. Part II

*Amal El Akkraoui<sup>a,b</sup>, T. Rieckh<sup>c</sup>, L. Takacs<sup>a,b</sup>, J. Sjoberg<sup>c</sup>, G. Partyka<sup>a,b</sup>,  
R. Gelaro<sup>a</sup>, and R. A. Anthes<sup>c</sup>*

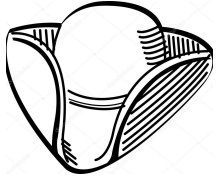
*<sup>a</sup>GMAO, Earth Sciences Division, Sciences and Exploration Directorate, NASA/GSFC.*

*<sup>b</sup>Science Systems and Applications, Inc. (SSAI)*

*<sup>c</sup>University Corporation for Atmospheric Research (UCAR)*

102<sup>nd</sup> AMS Annual Meeting

26th Conference on Integrated Observing and Assimilation Systems for the Atmosphere, Oceans, and Land Surface (IOAS-AOLS)  
27 January 2022



# Three corners for error estimation

- The theory of the three-cornered hat method was detailed in the previous talk (part I);
- Use of 3CH with gridded datasets (i.e., ERA5, MERRA-2, JRA55, ECOPS...);
- Examples of 3CH application in reanalysis feature testing and NWP upgrade evaluations.

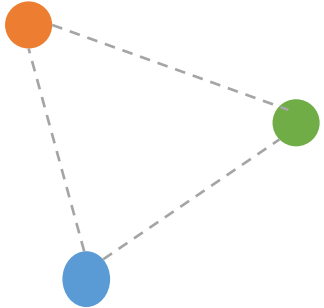
## Why use gridded datasets?

Instead of collocated profiles in observation space, we can use the method on gridded datasets to get error variance [estimates on model grid](#), for [all variables](#), including the unobserved ones.

**Caveat:** Choosing appropriate corners takes an educated guess about the error correlations and trials and errors.

At GMAO, we want to use the 3CH routinely as a diagnostic tool for evaluation of NWP and reanalysis developments. The adequate choice of corners and the robustness of results are critical.

# 3CH Formulation



$$X = \text{Truth} + b_x + \varepsilon_x$$

$$Y = \text{Truth} + b_y + \varepsilon_y$$

$$Z = \text{Truth} + b_z + \varepsilon_z$$

Variance of the random error

$$\sigma_{err}^2(X) = \sigma^2(\varepsilon_x)$$

Could these terms be neglected?

$$\sigma^2(\varepsilon_x) = \frac{1}{2}(\sigma^2(X - Y) + \sigma^2(X - Z) - \sigma^2(Y - Z)) + \frac{1}{N} \sum \varepsilon_x \varepsilon_y + \frac{1}{N} \sum \varepsilon_x \varepsilon_z - \frac{1}{N} \sum \varepsilon_y \varepsilon_z$$

Can be computed explicitly

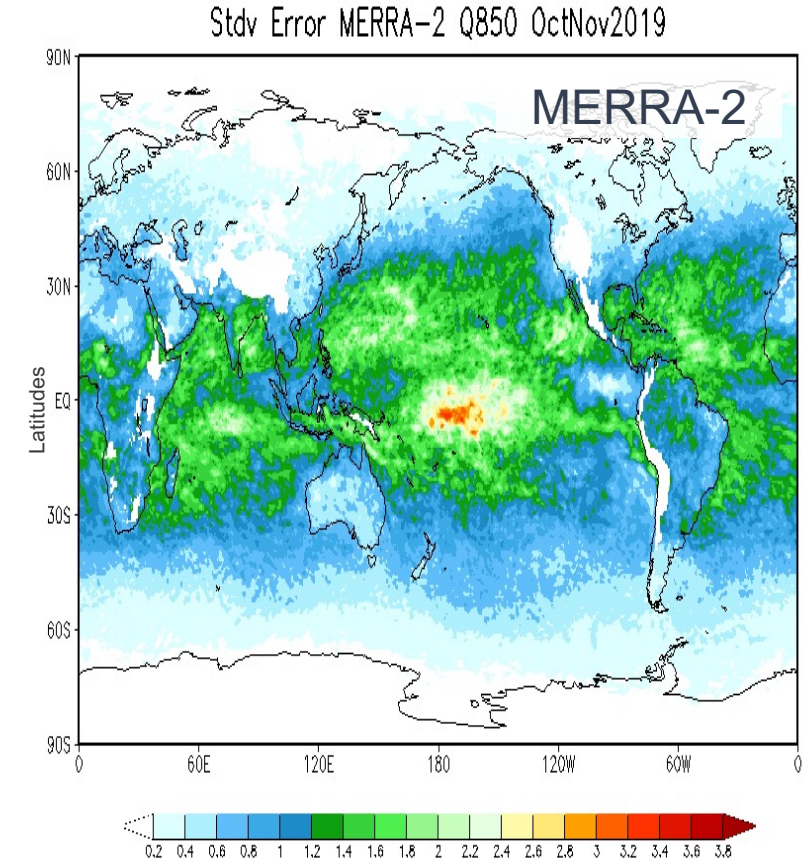
Terms related to the correlations between the random errors

- We get estimates of error variances for the three states (corners) without the need for the true state.
- Choice of the three corners assumes negligible error correlations. This is where it gets tricky!

## 3CH with gridded data

Standard deviation 3CH estimated error in specific humidity, 850hPa (g/kg)

- Horizontal plots of error standard deviations to inform on regions of large error estimates.

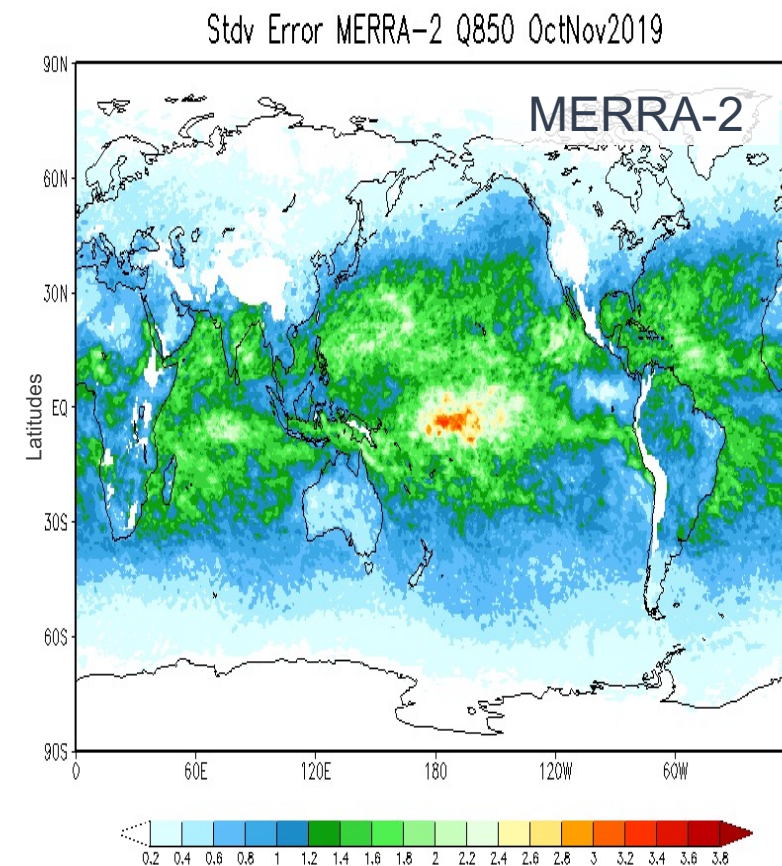
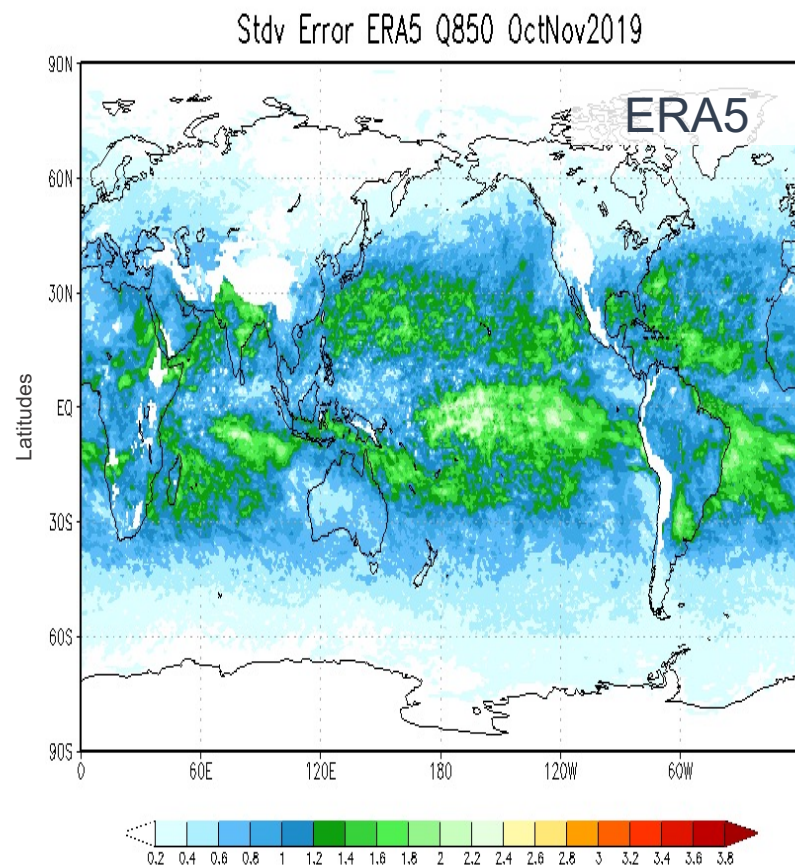


Large MERRA-2 error standard deviations localized over ocean in the tropics.

## 3CH with gridded data

Standard deviation 3CH estimated error in specific humidity, 850hPa (g/kg)

- Horizontal plots of error standard deviations to inform on regions of large error estimates.
- Direct comparison of estimates between datasets.



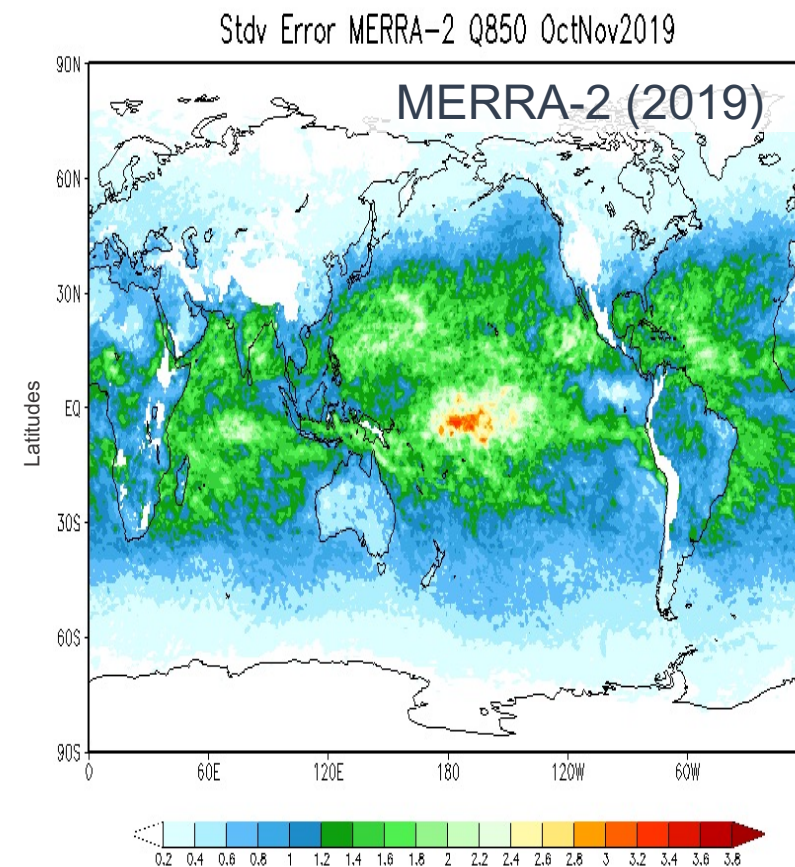
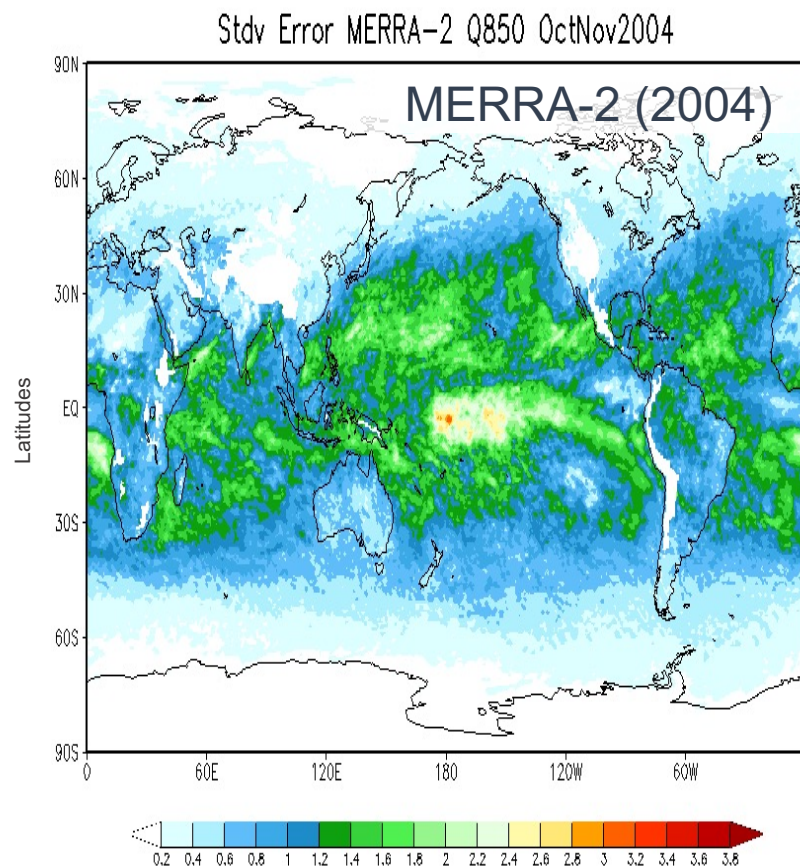
MERRA-2 error standard deviations larger than those of ERA5 mostly in the tropics.



## 3CH with gridded data

Standard deviation 3CH estimated error in specific humidity, 850hPa (g/kg)

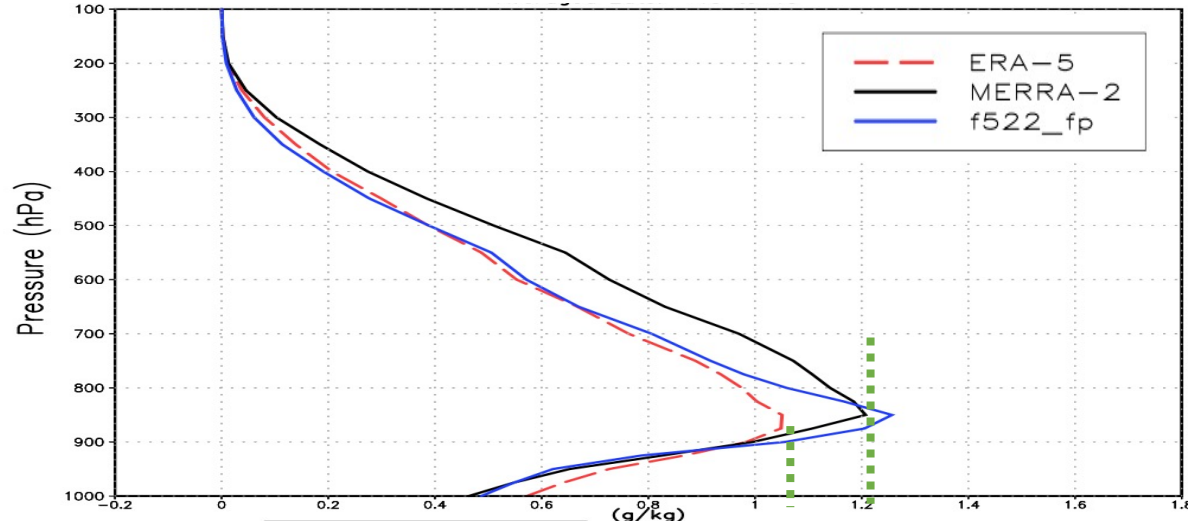
- Horizontal plots of error standard deviations to inform on regions of large error estimates.
- Direct comparison of estimates between datasets.
- Comparison of error evolution in time (as described in part I of this talk).



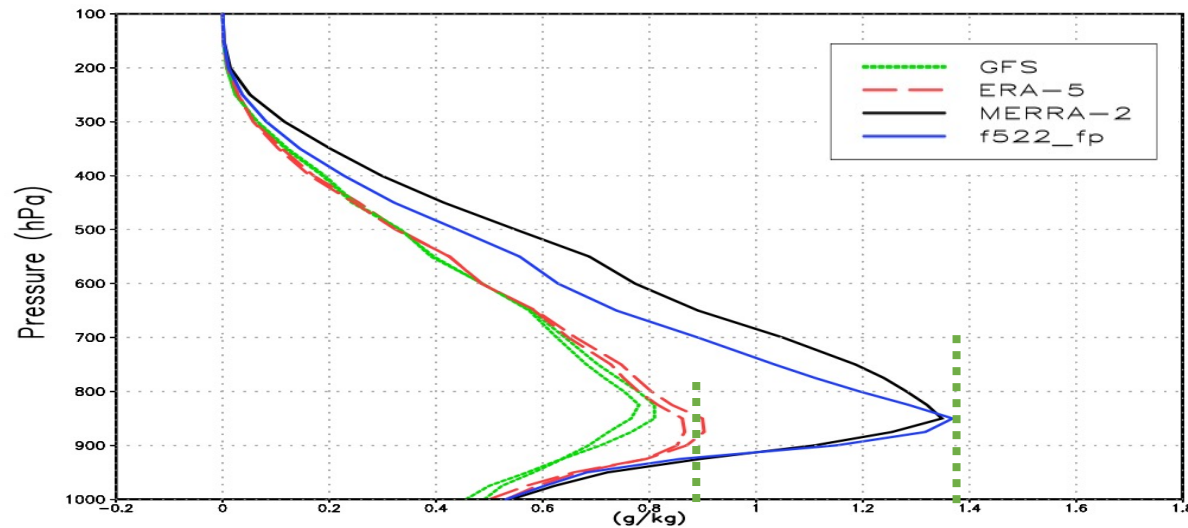
Error standard deviations larger in the later period of MERRA-2.

# Choice of adequate corners

Standard deviation 3CH estimated error for tropical specific humidity (g/kg)

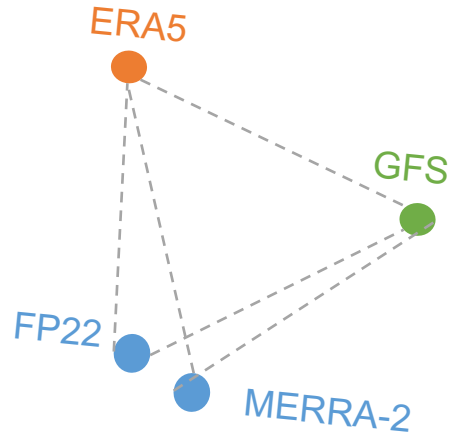


FP22: GEOS version 5.22  
MERRA-2: GEOS version 5.12



Error correlations between MERRA-2 and FP22 leads to:

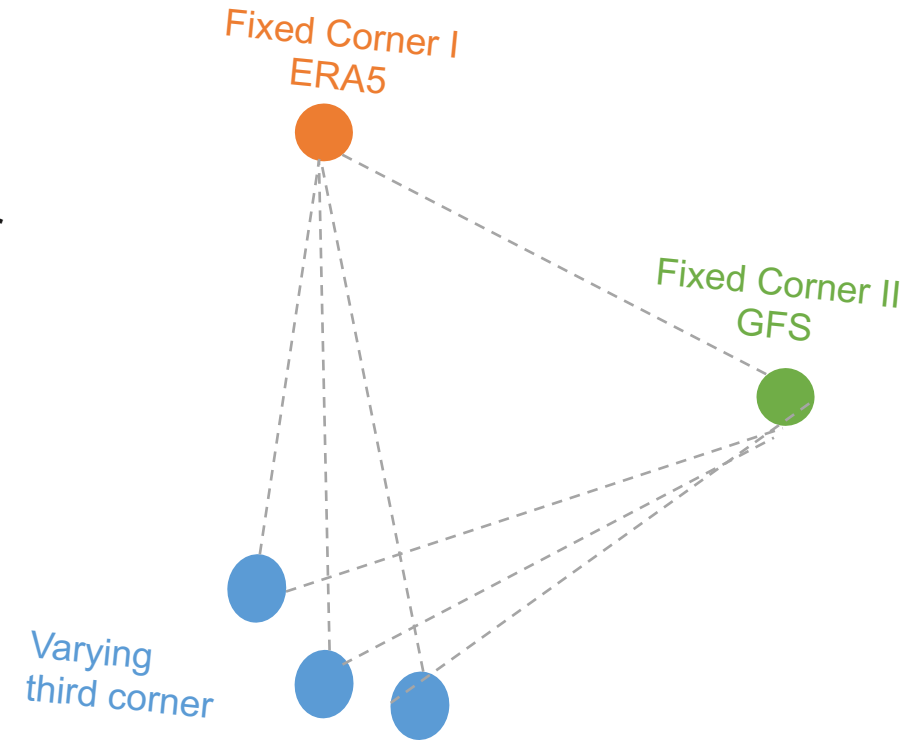
- Over-estimation of ERA5 error stdv.
- Under-estimation of MERRA-2 error stdv.



# Applications of the 3CH method at GMAO

We want to use the 3CH routinely as a diagnostic tool for evaluation of NWP and reanalysis developments.

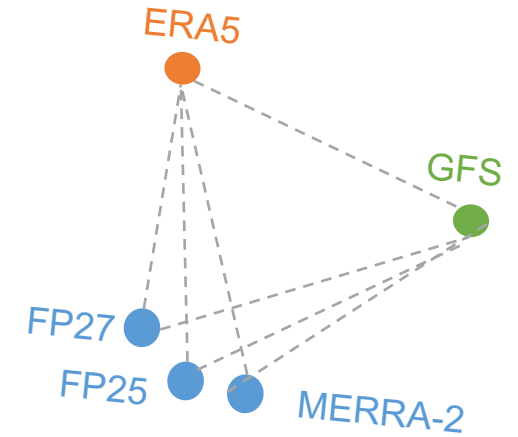
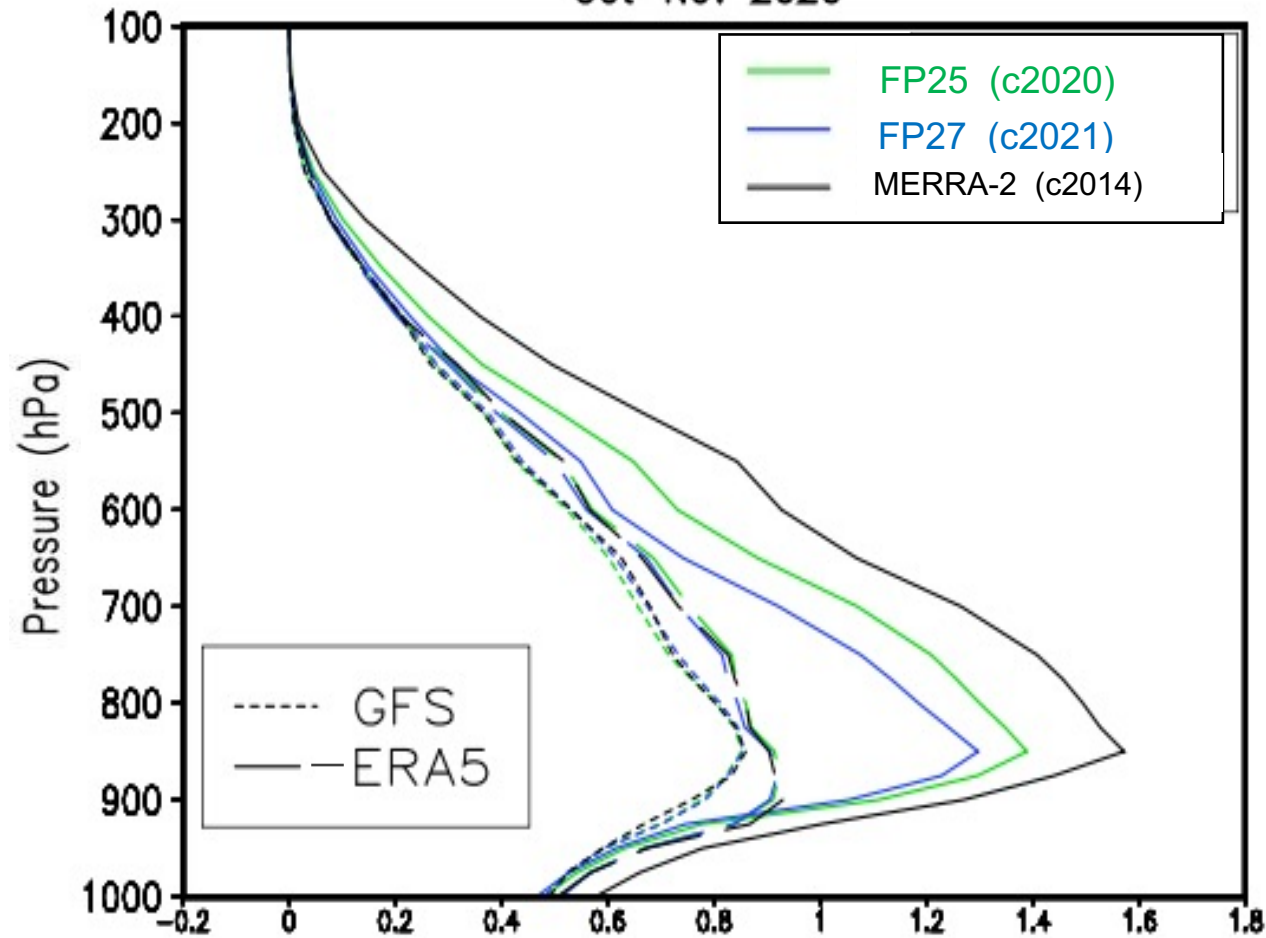
It's not about comparing error estimates with ERA5/GFS but comparing errors within variants on the third corner.





# Applications of the 3CH method at GMAO

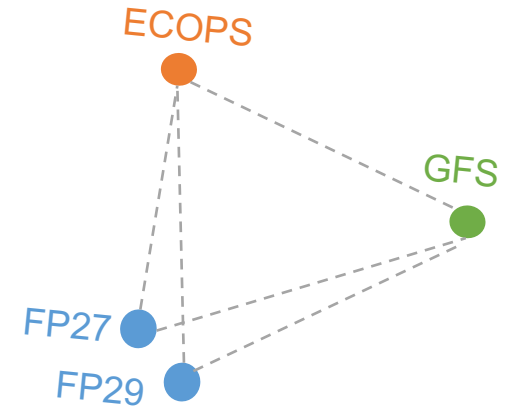
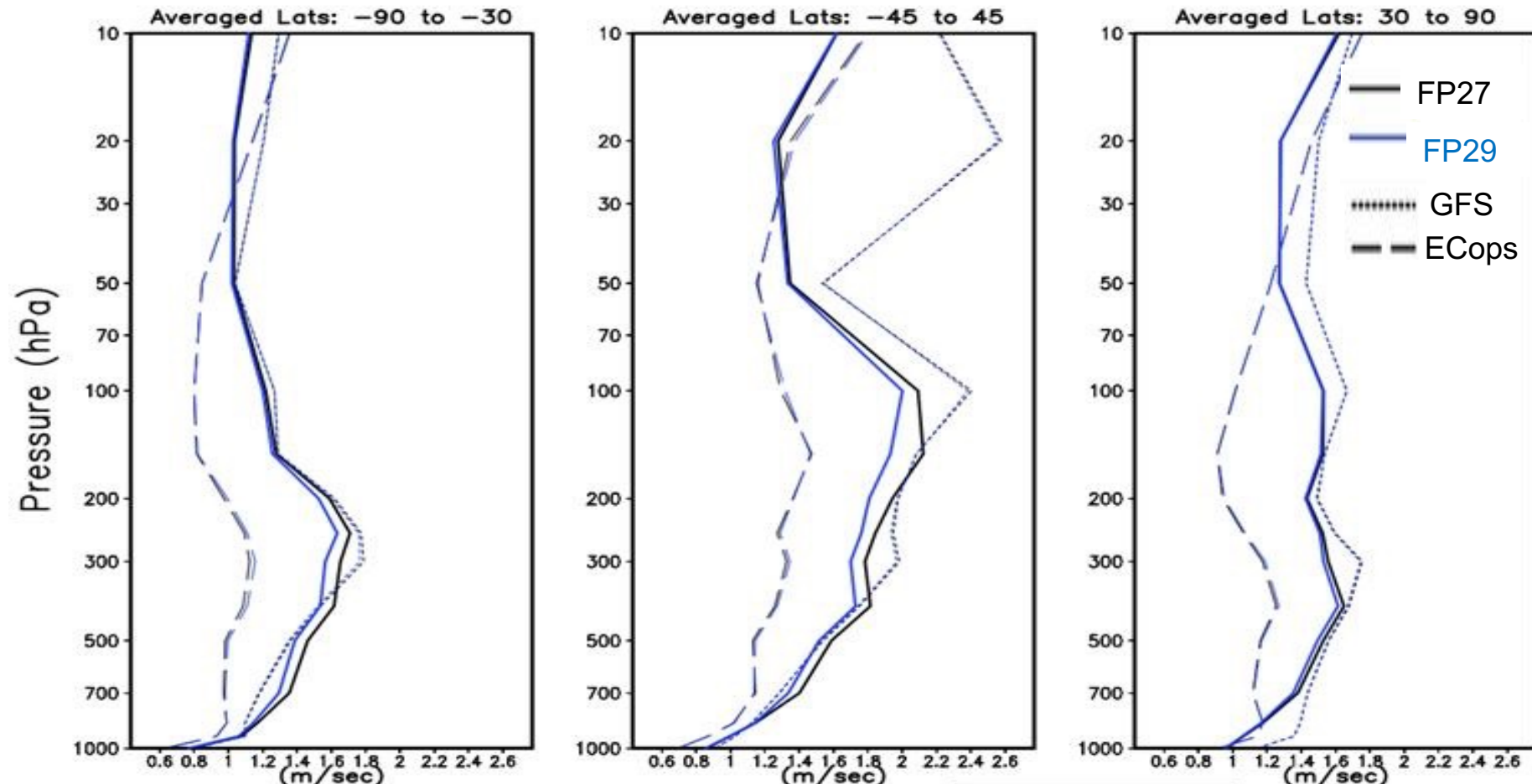
Standard deviation 3CH estimated error for recent versions  
of GEOS-FP – Tropical Specific humidity (g/kg)  
Oct–Nov 2020



Improvements in recent versions of GEOS system are corroborated by other routine diagnostic metrics.

# Applications of the 3CH method at GMAO

Standard deviation 3CH estimated error for recent versions  
of GEOS-FP Zonal Wind (m/s)



GEOS Version 5.29 introduces changes to the treatment of GOES-R winds. The 3CH estimates of wind error stdv capture the impact of this change.



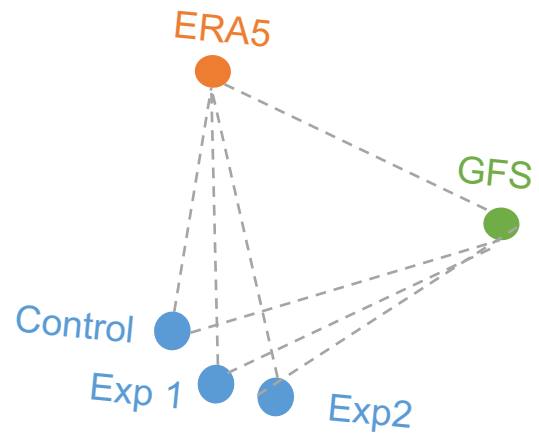
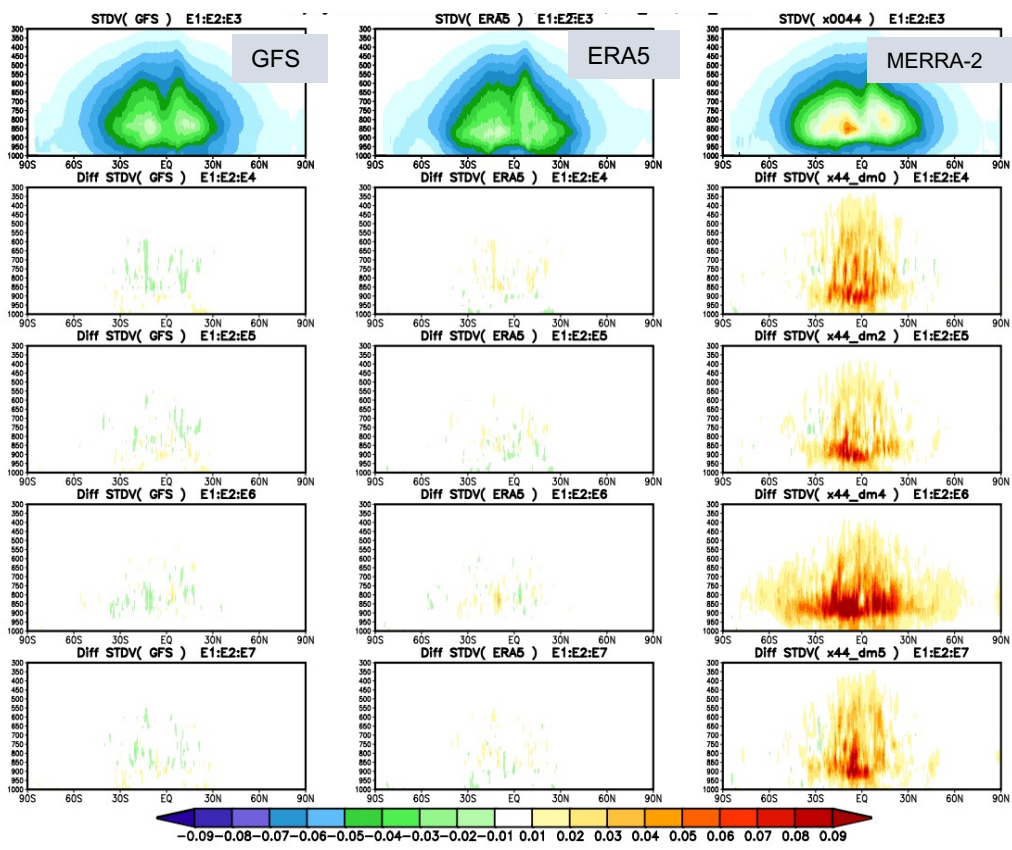
# Applications of the 3CH method at GMAO

## Ex: Dry mass constraint re-examination

3CH Specific Humidity  
Std.Dev. Difference from Control

Control  
case

Difference with control case



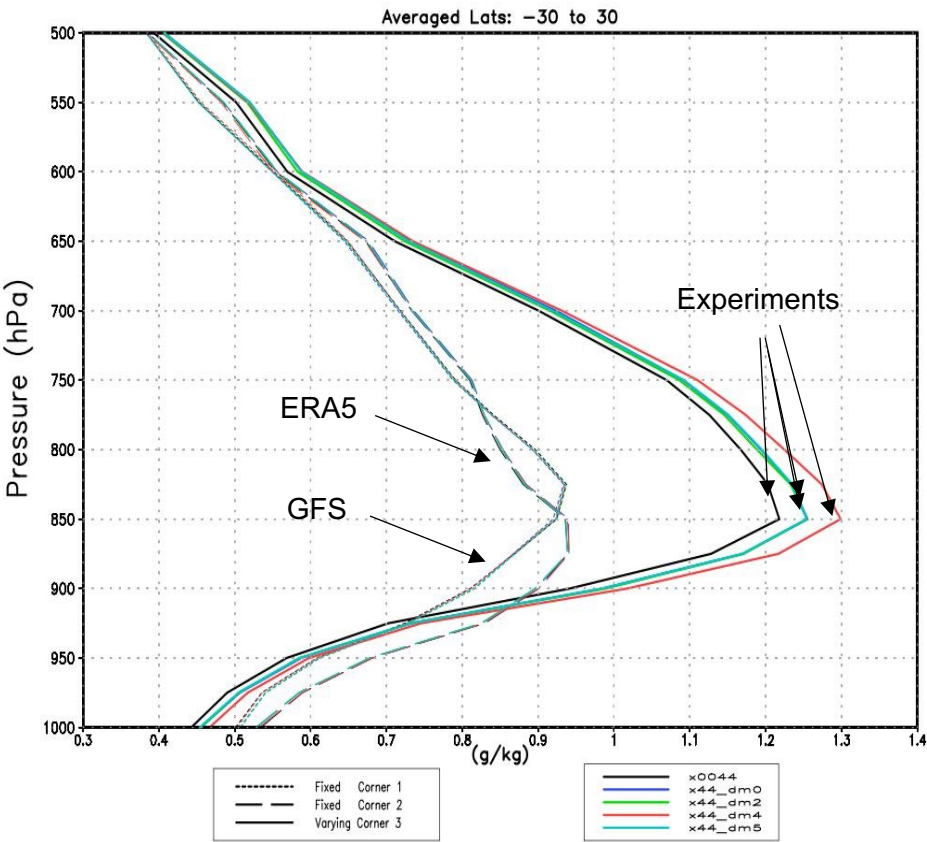
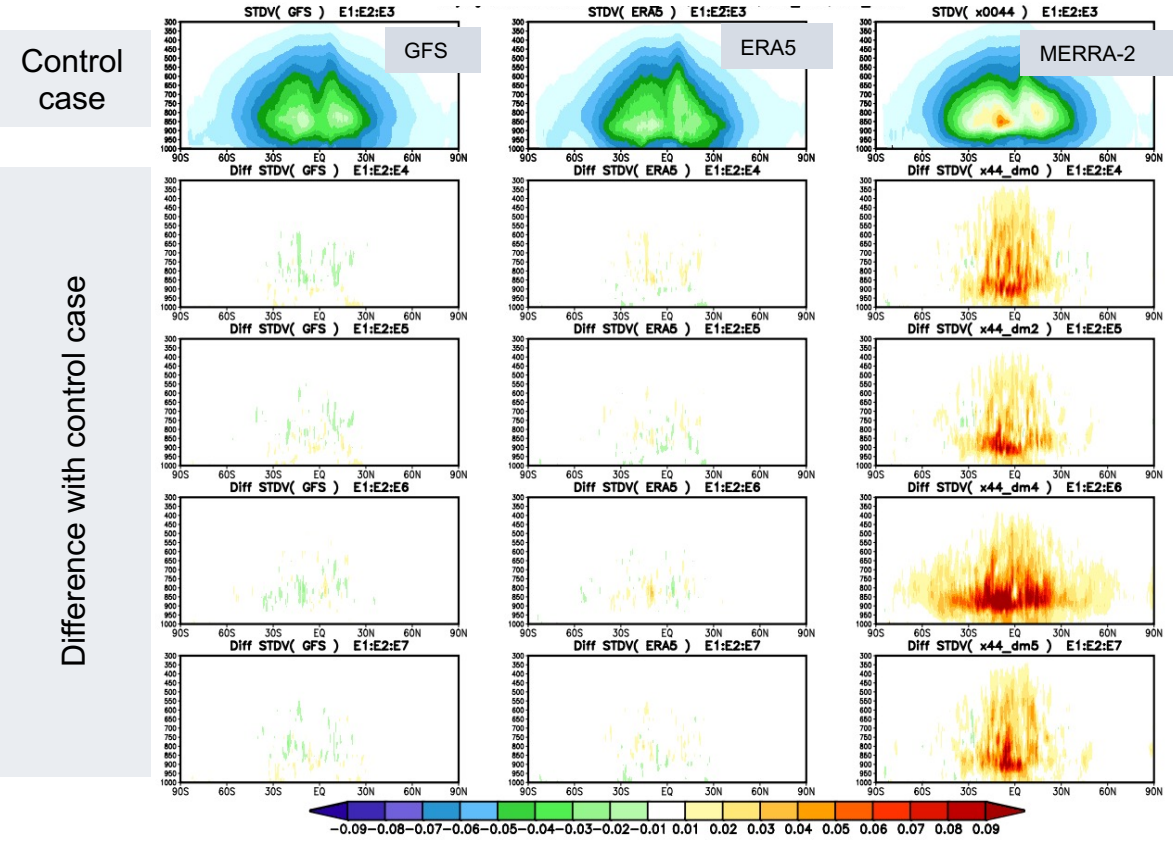


# Applications of the 3CH method at GMAO

## Ex: Dry mass constraint re-examination

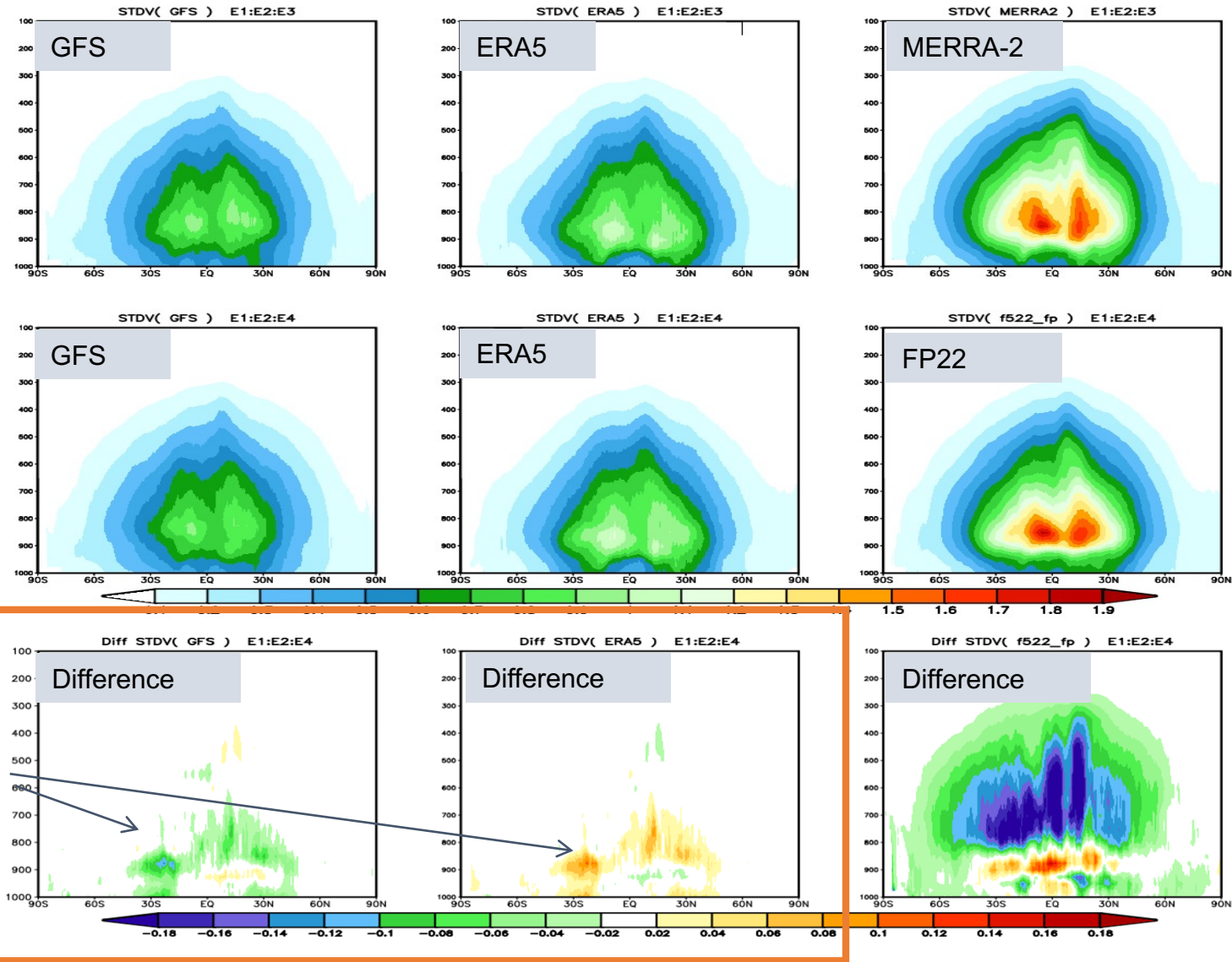
3CH Specific Humidity Std.Dev.  
Difference from Control

3CH Specific Humidity Std.Dev.  
Profiles averaged over lat -30 and 30.





# On the robustness of the 3CH method





# Summary

- The three-cornered hat method is proving to be a strong diagnostic tool for the evaluation of NWP and reanalysis developments.
- We have been using it at GMAO directly with gridded datasets which allows for error variance estimation on model grids and of all variables.
- Results confirm the peculiar behavior MERRA-2 specific humidity shown in the previous talk (part I). The 3CH was used to assess candidate systems for the upcoming reanalysis.
- The choice of appropriate corners is critical. Accuracy of the results rests of the veracity of the underlying assumption about error correlations.
- The 3CH method provides estimates of the variances of the random part of the total error. The bias is not addressed and should be evaluated separately.
- Work on quantifying the robustness of the method with different scenarios and datasets is ongoing.